# Phase Equilibria and the Thermodynamics of Coexisting Phases in the System Iron-Lithium-Oxygen\*

# YU. D. TRETYAKOV, N. N. OLEYNIKOV, YU. G. METLIN, AND A. P. ERASTOVA

Department of Chemistry, Moscow State University, Moscow, USSR

Received November 12, 1971

Phase equilibria in the system  $Fe_2O_3$ - $FeO-Li_{0.5}Fe_{0.5}O$  have been studied over a broad range of temperatures (900-1200°C) and partial pressure of oxygen (10<sup>-15</sup> – 1 atm) both by quench methods and solid-electrolyte electromotive force measurements together with chemical and X-ray analyses. Equilibrium conditions have been determined for the formation of iron lithium spinel,  $Li_xFe_{3-x}O_{4+\gamma}$ , which changes its non-stoichiometric character according to the amount of oxygen present from an excess of the latter ( $\gamma > 0$ ) when  $x \approx 0$  to a deficit ( $\gamma < 0$ ) when x approaches 0.5. The activity of the components in coexisting spinel and wüstite phases has been calculated. It is shown that solutions of lithium ferrite with magnetite in equilibrium with wüstite are characterized by small deviations from ideality—positive in the region which is rich in magnetite and negative in the concentration range bordering on lithium ferrite. Furthermore,  $\Delta H$  is approximately zero, i.e., the solutions are athermal. Solutions of lithium ferrite and magnetite in equilibrium with hematite and solutions of wüstite and lithium orthoferrite in equilibrium with the spinel phase are characterized by marked deviations from ideality.

#### Introduction

Among the ferrites with spinel structure special attention is given to the formation of a polycrystalline lithium ferrite with a square hysteresis loop having a highest Curie point of  $670^{\circ}C(l)$ and retaining its superstructure up to  $750^{\circ}C(2)$ . In spite of numerous investigations designed to establish the synthesis conditions, the kinetics of formation, and the thermal working of the lithiumcontaining ferrites (3-8), many peculiarities of the behavior have not been satisfactorily explained. It is known, for example, that the squareness of the hysteresis loop of lithium-containing ferrites is extremely sensitive to the value of the oxygen partial pressure at the thermal working conditions. However, it is not clear whether this phenomenon is related to phase decomposition of spinel (6) or to a change in the concentration of point defects within the limits of a monophase area (9).

The solution of this and a series of related problems should contribute to the understanding

\* Original manuscript received in Russian. A copy is available on written request to the editors.

of phase equilibria and thermodynamic properties of coexisting phases in the Fe-Li-O system. The clarification of the equilibrium conditions for formation of iron-lithium spinel, particularly the dependence of nonstoichiometry on the oxygen partial pressure and temperature, obviously presents considerable interest. Data in the literature on phase equilibria in the Fe-Li-O system give little information. From Refs. (6 and 7), it follows that in the Fe-Li-O system it is possible to have formation of two phases of variable composition: one with spinel structure, the other with NaCl structure. The first of these is a solid solution based on magnetite  $Li_xFe_{3-x}O_{4+\gamma}$  $(0 < x \le 0.5)$ ; the second, a solution based on wüstite  $\text{Li}_{z}\text{Fe}_{1-z}\text{O}_{1+\delta}$  (0 < z < 0.5). According to the data in Ref. (7), decomposition of the spinel phase leads to formation of a wüstite solution richer in lithium than the spinel. Relatively recently (10) the existence of yet another compound, LiFe<sub>5</sub>O<sub>8</sub>, in the binary system  $Li_2O-Fe_2O_3$  has been established.

The scope of the present investigation was limited to the study of phase equilibria in the

Copyright © 1972 by Academic Press, Inc. All rights of reproduction in any form reserved. high-oxygen regions of the Fe-Li-O diagram and to the determination of the thermodynamic properties of the coexisting phases.

## **Experimental Part**

For studying the phase equilibria two procedures were used:

(a) quenching specimens after equilibration with gas phase having a particular partial pressure of oxygen;

(b) an electromotive force method using a solid electrolyte with purely anionic-oxygen conductivity.

Starting preparations. The starting oxide mixtures for the investigation of equilibria by the quench method were obtained from lithium orthoferrite and hematite, taken in the proportions shown in Table I and homogenized by heating for 2 hr at 900°C. The orthoferrite, in its turn, was prepared according to the reaction

$$Li_2CO_3 + Fe_2O_3 = 2LiFeO_2 + CO_2$$
, (1)

by heating at 700°C for 3 hr. This use of orthoferrite as an intermediate enabled us to reduce significantly the loss of lithium during the process of preparing the starting preparations (3).

#### TABLE I

Composition of Starting Oxide Mixtures for Investigating the Equilibria by the Dynamic Method

N <sub>LiFeO2</sub>	N <sub>Fe2O3</sub>	x in formula $\text{Li}_x\text{Fe}_{3-x}\text{O}_{4+\gamma}$	
0.025	0.975	0.0375	
0.050	0.950	0.0750	
0.075	0.925	0.1125	
0.100	0.900	0.1500	
0.125	0.875	0.1875	
0.150	0.850	0.2250	
0.200	0.800	0.3000	
0.250	0.750	0.3750	
0.267	0.733	0.4000	
0.283	0.717	0.4250	
0.300	0.700	0.4500	
0.317	0.683	0.4750	
0.333	0.667	0.5000	
0.400	0.600	0.6000	
0.500	0.500	0.7500	
0.700	0.300	1.0500	
0.800	0.200	1.2000	
0.900	0.100	1.3500	

For investigating the phase equilibria using the EMF method, several series of samples were prepared:

1. Samples with overall composition  $\text{Li}_z\text{Fe}_{1-z}\text{O}_{1+\delta}$ , where z = 0, 0.12, 0.24, 0.36, 0.50 and  $\delta = 0.13, 0.09, 0.06, 0.03, 0$ , respectively, were obtained from lithium orthoferrite, hematite and "FeO" by the reaction:

$$z\text{LiFeO}_2 + (1 - 2z - 2\delta)\text{FeO} + \delta\text{Fe}_2\text{O}_3 = \text{Li}_z\text{Fe}_{1-z}\text{O}_{1+\delta}.$$
 (2)

2. Samples of the composition  $\text{Li}_t \text{Fe}_{4-t} O_5$ , where t = 0, 0.14, 0.28, 0.42, 0.56, 0.70, 0.84, 1.00, were obtained by the reaction:

$$t \operatorname{LiFeO}_2 + 2(1-t)\operatorname{FeO} + \operatorname{Fe}_2\operatorname{O}_3 = \operatorname{Li}_t \operatorname{Fe}_{4-t}\operatorname{O}_5.$$
(3)

3. Samples of the composition  $\text{Li}_x\text{Fe}_{3-x}O_{3.99}$ , where x = 0, 0.07, 0.14, 0.20, 0.27, 0.34, 0.42, 0.50, were obtained from lithium ferrite and magnetite by the reaction:

$$2x \text{Li}_{0.5} \text{Fe}_{2.5} \text{O}_{3.99} + (1 - 2x) \text{Fe}_{3} \text{O}_{3.99} = \text{Li}_{x} \text{Fe}_{3-x} \text{O}_{3.99}.$$
 (4)

4. Samples of the composition  $\text{Li}_{y}\text{Fe}_{5-y}O_{7}$ , where y = 0, 0.07, 0.14, 0.20, 0.27, 0.34, 0.43, 0.50, were obtained from lithium orthoferrite, hematite and FeO by the reaction:

$$y\text{LiFeO}_2 + (1-2y)\text{FeO} + 2\text{Fe}_2\text{O}_3 = \text{Li}_y\text{Fe}_{5-y}\text{O}_7$$
(5)

Wüstite of the composition "FeO" and magnetite "Fe<sub>3</sub>O<sub>3.99</sub>" were prepared in turn from carbonyl iron and hematite, mixtures of which were pressed into pellets ( $P = 1.6 \ T/cm^2$ ) and heated in evacuated quartz ampoules at 900°C for a period of 24 hr. Chemical analysis of the reaction products for Fe<sup>2+</sup> and Fe<sup>3+</sup> confirmed the presence of wüstite and magnetite of the required composition.

Lithium ferrite was obtained from hematite and lithium orthoferrite by reacting the powder mixture, which was carefully mixed in an agate mortar under a layer of ether for 2 hr, at a temperature of 900°C and a partial pressure of oxygen of 0.016 atm. for 20 hr.

Reactions (2)–(5) were carried out on pelletized mixtures at 900°C for 24 hr in evacuated quartz ampoules. For carrying out reactions (3) and (4) at 1100°C, double quartz ampoules were used with metal titanium chips in the space between. The titanium precluded any possible oxidation of the specimens in the inner ampoule as a result of air flow from the outside.

Investigation of equilibria by the quench method (11, 12). The setup for investigating equilibria by the quench method is shown schematically in Fig. 1. The platinum container (1) with an 0.6-g specimen is attached to a special suspension (2) in the center of the quartz reactor (3), which in turn is placed in a vertical furnace (4). The construction of the furnace permitted 4 reactors to be in place simultaneously. The specimens were heated at constant temperature in a gas medium with fixed oxygen partial pressure for the period of time needed to attain equilibrium between the gas and condensed phases. After the burning through of the suspension filament (5), the specimens were quenched by being dropped into receiver (6), containing liquid nitrogen. The temperature in the zone of the oxides was measured with a Pt-Pt/Rh thermocouple (7). On the basis of preliminary experiments the times selected for holding the specimens isothermally to guarantee establishment of equilibrium between gas and condensed phases were as follows: 900°C, 20 hr; 1000°C, 10 hr; 1100°C, 6 hr; 1200°C, 4 hr.

Experiments were carried out in gas mixtures having oxygen partial pressures of 1, 0.21, 0.016, and 0.001 atm as well as with the oxygen partial

FIG. 1. Diagram of the apparatus for investigating equilibria by the quench method.

pressure created by the thermal dissociation of carbon dioxide. The oxygen content of all the gas mixtures was determined by measurement of the EMF of a cell with divided gas space:

gas mixture  
with measured 
$$(Pt)|ZrO_2(CaO)|(Pt)$$
, air.  
pressure of oxygen (6)

All the gas mixtures used were dried with concentrated sulfuric acid together with granulated anhydrous  $Mg(CIO_4)_2$ . The latter was contained in three consecutively connected drying columns. Such precautions were taken because even small amounts of water vapor in the gas phase are enough to give nonequilibrium removal of lithium oxide from the condensed phase in the form of LiOH (13).

Phase analysis of the quenched specimens was carried out by X-rays using Debye's method with  $FeK_{\alpha}$  radiation. Lattice constants were determined photographically and on a diffractometer with a possible error of  $\pm 0.001$  Å.

As has been shown earlier (14), for compositions  $\text{Li}_x\text{Fe}_{3-x}O_{4+\gamma}$  the quantity  $\gamma$  can be determined by the formula

$$\gamma = \frac{1}{2} \frac{1 - 2x - pM}{1 + 8p}, \tag{7}$$

where p is the number of gram-ions of  $Fe^{2+}$  in 1 g of the dissolved condensed phase and M is the "molecular weight" of the composition  $Li_xFe_{3-x}O_4$  ( $\gamma = 0$ ). In order to preclude oxidation of the  $Fe^{2+}$ , the quenched specimens were brought to solution in sealed glass ampoules filled with an inert atmosphere. The determination of the  $Fe^{2+}$  content was done by potentiometric titration with a solution of cerium(IV) sulfate.

Investigation of equilibria by the EMF method. To determine the chemical potential of oxygen in coexisting spinel and wüstite phases the EMF method was used with a solid electrolyte  $ZrO_2(CaO)$  having anion-oxygen conductivity. The construction of the cells with divided and strictly defined space over the electrodes has been described by one of the authors (15). The basic feature of the cells used (Fig. 2) is the tube (1), a gas-impermeable tube of zirconium dioxide stabilized with calcium oxide. The tube serves as an electrolyte with oxygen conductivity and at the same time as a working chamber that separates the electrode being investigated (3) from the standard (2). The powdered specimen was placed in the platinum container (3), which served simultaneously as the inner electrode. To eliminate





FIG. 2. Diagram of the cell with divided electrode space for measurement of the electromotive force.

contact potentials, the sample was insulated from the platinum electrode by the corundum cup (4). After introduction of the specimen into the working chamber, the latter was evacuated to a residual pressure of  $10^{-3}$  mm Hg, flushed, and finally filled with pure helium.

For investigating the specimens of  $\text{Li}_t \text{Fe}_{4-t} O_5$  where t = 0.70 and 0.34, air was used as the comparison electrode; for investigating the specimens of  $\text{Li}_t \text{Fe}_{4-t} O_5$  where t = 0, 0.14, 0.33, 0.42 and 0.56, equilibrium mixtures of FeO/Fe<sub>3</sub>O<sub>4</sub> served as the electrode. Experiments were carried out over the interval 800–1000°C.

The chemical potential of the oxygen over the coexisting phases was calculated from the equilibrium values of the EMF by well-known thermodynamic relations. For the electro-chemical elements:

standard				investigated
oxygen-	( <b>D</b> +)	solid	( <b>D</b> +)	oxygen-
containing	(rij	electrolyte	(r),	containing
electrode,				electrode

the electromotive force is given by

$$E = \frac{1}{4F} \int_{\mu'_{O_2}}^{\mu_{O_2}} t_{ion} \, d\mu_{O_2}, \qquad (8)$$

where  $\mu'_{O_2}$  and  $\mu''_{O_2}$  are the chemical potentials of the oxygen on the two sides of the electrolyte, Fis the Faraday number, and  $t_{ion}$  is the transport number of the oxygen ions. If  $t_{ion} = 1$ , then from Eq. (8) it follows that

$$\mu_{O_2}'' = \mu_{O_2}' + 4EF, \qquad (9)$$

or with the substitution

$$\mu_{O_2} = \mu_{O_2}^0 + RT \ln p_{O_2} \tag{10}$$

we get

$$p''_{O_2} = p'_{O_2} \exp\left(\frac{4EF}{RT}\right)$$
 (11)

where  $p'_{O_2}$  and  $p''_{O_2}$  are the equilibrium oxygen pressures over the reference and investigated electrodes, respectively.

### **Basic Results and Discussion**

The results of investigating phase equilibria by the quench method are represented in Figs. 3-6 (chemical analysis data) as well as in Figs. 7 and 8 (X-ray analysis data). It is easy to see that the specimens of overall composition  $Li_xFe_{3-x}O_{4+\gamma}$  over the range of temperature (900-1200°C) and oxygen partial pressure studied fall into 3 groups:

a. Two-phase mixtures of hematite and spinel. On the  $\gamma = f(x)$  curves, the rectilinear sections originating from the points with  $\gamma = 0.5$  and x = 0 correspond to these mixtures. These straight lines are actually tie-lines of coexisting phases, one of which is pure hematite and the other is iron-lithium spinel of a variable composition given by the point of intersection of the tie-line with the abscissa axis. On the a = f(x) curves, the two-phase mixtures of hematite and spinel correspond to the rectilinear segments parallel to the abscissa axis; these characterize the invariability of the spinel composition along the individual tie-lines.



FIG. 3. Dependence of  $\gamma = f(x)$  in Li<sub>x</sub>Fe<sub>3-x</sub>O<sub>4+y</sub> at 900°C.



FIG. 4. Dependence of  $\gamma = f(x)$  in Li<sub>x</sub>Fe<sub>3-x</sub>O<sub>4+ $\gamma$ </sub> at 1000°C.

b. Single-phase iron-lithium spinel of variable composition. The curvilinear sections on the  $\gamma = f(x)$  diagrams (Fig. 3-6) and the sharp change in lattice constant as a function of x (Figs. 7 and 8) correspond to this phase. It is noteworthy that the range of composition (value of x) corresponding to the single-phase spinel increases in proportion to an increase in temperature. Furthermore, the oxygen nonstoichiometry of the spinel changes its character with different values of x. For compositions close to pure lithium ferrite,



FIG. 5. Dependence of  $\gamma = f(x)$  in Li<sub>x</sub>Fe<sub>3-x</sub>O<sub>4+ $\gamma$ </sub> at 1100°C.



FIG. 6. Dependence of  $\gamma = f(x)$  in Li<sub>x</sub>Fe<sub>3-x</sub>O<sub>4+y</sub> at 1200°C.

Li<sub>0.5</sub>Fe<sub>2.5</sub>O<sub>4</sub>, the spinel phase has a deficit of oxygen, whereas compositions rich in iron are characterized by an excess of oxygen, the latter reaching its maximum value at pure magnetite (x = 0).

c. Two-phase mixtures of spinel and wüstite phases of variable composition. On the  $\gamma = f(x)$ curves (Figs. 3–6), the rectilinear sections (tie-lines



FIG. 7. Dependence of a = f(x) for the compositions  $\text{Li}_x \text{Fe}_{3-x} O_{4+\gamma}$  at (a) 900°C and (b) 1000°C.



FIG. 8. Dependence of a = f(x) for the compositions  $\text{Li}_x \text{Fe}_{3-x} O_{4+\gamma}$  at (a) 1100°C and (b) 1200°C.

of coexisting phases) found below the axis of the abscissa correspond to these mixtures. In Figs. 7 and 8, which show the dependence a = f(x), the rectilinear sections characterizing the invariability of spinel composition along the individual tie-lines correspond to mechanical mixtures of coexisting spinel and wüstite phases.

To construct the isothermal sections of the state diagram for the system

the composition of the condensed phase  $Li_xFe_{3-x}O_{4+\gamma}$  was calculated in mole percent (mole fraction) of the respective components according to the following formulas:

$$N_{\rm Li_{0.5}Fe_{0.5}O} = \frac{2x}{2-\gamma},$$
 (12)

$$N_{\rm FeO} = \frac{1 - 2x - 2\gamma}{2 - \gamma},\tag{13}$$

$$N_{\mathrm{Fe}_{2}\mathrm{O}_{3}} = \frac{1+\gamma}{2-\gamma}.$$
 (14)

The results of these calculations are represented by the heavy lines in Figs. 9-12.

Inasmuch as the quench method did not allow us to map a significant portion of the two-phase spinel-wüstite region, the diagram was filled in with data obtained from the EMF method. To this end, the equilibrium oxygen pressures were measured for specimens of composition  $Li_t Fe_{4-t}O_5$  lying inside the two-phase region (broken lines in Figs. 9–11). Data from the X-ray



FIG. 9. Isothermal section of the state diagram for the system  $Fe_2O_3$ -FeO-Li<sub>0.5</sub>Fe<sub>0.5</sub>O at 900°C. (•)  $p_{O_2} = 2.7 \times 10^{-6}$  atm; (×)  $1.0 \times 10^{-3}$  atm; (△)  $1.6 \times 10^{-2}$  atm.

analysis confirmed the two-phase nature of the indicated specimens. Furthermore, comparison of the spinel constant with the base-line curve (Fig. 13) for specimens of compositions  $\text{Li}_z\text{Fe}_{1-z}O_{1+\gamma}$  and  $\text{Li}_x\text{Fe}_{3-x}O_{3.99}$  allowed us to fix the position of the tie-lines on the diagram (tie-lines are plotted with thin lines).

Some error in the determination of the position of the tie-lines can be related to the arbitrariness of the assumption that the spinel lattice constant at composition  $Me_3O_{3.99}$  corresponds to that for the low-oxygen limit of the spinel field, the posi-



FIG. 10. Isothermal section of the state diagram for the system  $Fe_2O_3$ -FeO-Li<sub>0.5</sub>Fe<sub>0.5</sub>O at 1000°C. (•)  $p_{O_2} = 1.2 \times 10^{-5}$  atm; (×)  $1.0 \times 10^{-3}$  atm; ( $\triangle$ )  $1.6 \times 10^{-2}$  atm; ( $\bigcirc$ )  $2.1 \times 10^{-1}$  atm.



FIG. 11. Isothermal section of the state diagram for the system  $\text{Fe}_2\text{O}_3$ -FeO-Li<sub>0.5</sub>Fe<sub>0.5</sub>O at 1100°C. (**•**)  $p_{\text{O}_2} = 4.6 \times 10^{-5}$  atm; ( $\times$ ) 1.0  $\times$  10<sup>-3</sup> atm; ( $\triangle$ ) 1.6  $\times$  10<sup>-2</sup> atm; ( $\bigcirc$ ) 2.1  $\times$  10<sup>-1</sup> atm.

tion of which was established only for compositions rich in lithium. In order to convince ourselves of the insignificance of the error related to this assumption, we compared (Fig. 13) the spinel lattice constant for two series of compositions,  $\text{Li}_x\text{Fe}_{3-x}\text{O}_{3.99}$  and  $\text{Li}_y\text{Fe}_{5-y}\text{O}_7$ , which lie along various sides of the one-phase spinel region. Within the limits of error at the temperatures chosen for the experiment, a change in the oxygen content of the spinel  $\text{Li}_x\text{Fe}_{3-x}\text{O}_{4+y}$  at constant x is not accompanied by a change in the lattice constant.



FIG. 12. Isothermal section of the state diagram for the system  $Fe_2O_3$ -FeO-Li<sub>0.5</sub>Fe<sub>0.5</sub>O at 1200°C. (×)  $p_{O_2} = 1.4 \times 10^{-4}$  atm; (□)  $1.6 \times 10^{-2}$  atm; (△)  $2.1 \times 10^{-1}$  atm; (○) 1.0 atm.



Li<sub>x</sub>Fe<sub>3-x</sub>O<sub>3,99</sub>, Li<sub>y</sub>Fe<sub>5-y</sub>O<sub>7</sub>, Li<sub>z</sub>Fe<sub>4-t</sub>O<sub>5</sub>, and Li<sub>z</sub>Fe<sub>1-z</sub>O<sub>1+ $\delta$ </sub> at 900°C ( $\bullet$ ) and 1100°C ( $\times$ ).

The results of investigating the phase equilibria in the system  $Fe_2O_3$ -FeO-Li<sub>0.5</sub>Fe<sub>0.5</sub>O were used for a thermodynamic analysis of the components in the various phases. As has been shown previously (16), the activity of any combination of components in the heterogeneous region of a system A-B-C can be calculated by the following formula:

$$\log a_{A_{r}B_{s}C_{t}} = -\frac{1}{j} \int_{(p_{C_{j}}^{0})'}^{(p_{C_{j}}^{0})'} \Delta d\log p_{O_{2}}$$
$$+ \frac{1}{j} \int_{(p_{C_{j}}^{0})''}^{p_{C_{j}}} \frac{r(km - fn) + s(en - kl) + t(fl - em)}{fl - em}$$
$$\times d\log p_{C_{1}}$$
(15)

Here  $(p_{C_j}^0)'$  is the vapor pressure of component C over the phase  $A_rB_sC_t$  that lies in the homogeneous region and  $(p_{C_j}^0)''$  is the vapor pressure of component C over  $A_rB_sC_{t+\Delta}$  that has the same relationship to components A and B as  $A_rB_sC_t$ but is in equilibrium with another condensed phase. The first term of Eq. (15) characterizes the activity of  $A_rB_sC_t$  in the phase  $A_rB_sC_{t+\Delta}$  and the second takes into account the change in the activity of  $A_rB_sC_t$  on integration along the two-phase boundary.

Equation (15) can be used for calculating the activity of any combination of components in any three-component system. For equilibrium

spinel and wüstite phases, the composition of which is expressed by the formulas  $\text{Li}_x\text{Fe}_{3-x}O_{4-\gamma}$  and  $\text{Li}_z\text{Fe}_{1-z}O_{1+\delta}$ , i.e.,

$$e = x \qquad l = z f = 3 - x \qquad m = 1 - z k = 4 - \gamma \qquad n = 1 + \delta$$

the activities of magnetite (r = 0, s = 3, t = 4) and lithium ferrite (r = 0.5, s = 2.5, t = 4) can be calculated according to the formulas

$$\log a_{\mathrm{Fe}_{3}\mathrm{O}_{4}} = -\frac{1}{2} \int_{(p_{\mathrm{O}_{2}}^{0})_{\mathrm{Fe}_{0}/\mathrm{Fe}_{3}\mathrm{O}_{4}}}^{p_{\mathrm{O}_{2}}} \times (1-3\delta) d\log p_{\mathrm{O}_{2}}$$
(16)

 $\log a_{\text{Li}_{0.5}\text{Fe}_{2.5}\text{O}_4} =$ 

$$\frac{1}{4} \int_{(p_{02}^{p})_{\text{Ll}_{0.5}\text{Fe}_{0.5}\text{O}/\text{Ll}_{0.5}\text{Fe}_{2.5}\text{O}_{4}}^{p_{02}} \times (1-3\delta) d\log p_{\text{O}_{2}} \quad (17)$$

taking into account that the oxygen nonstoichiometry is small ( $\gamma = 0$ ) on the low-oxygen boundary of the spinel field.

The results of calculating the activities with Eqs. (16) and (17) are presented in Fig. 14. It is easy to see that the spinel solid solutions of lithium ferrite with magnetite in equilibrium with wüstite solid solutions are characterized by small deviations from ideality—positive in the region rich in magnetite and negative in the range of concentrations bordering on lithium ferrite. The character of the dependence  $a_i = f(x)$  changes weakly with temperature; therefore,

$$\Delta H = \frac{\partial \ln a_i}{\partial (1/T)} = 0,$$

i.e., the solutions are athermal.



FIG. 14. Values of the activity of the components of spinel solution at the low-oxygen boundary. ( $\triangle$ ) 900°C; ( $\checkmark$ ) 1000°C; ( $\spadesuit$ ) 1100°C.



FIG. 15. Values of the activity of the components of spinel solution at the high oxygen boundary. (•)  $900^{\circ}C$ ; ( $\propto$ )  $1000^{\circ}C$ ; ( $\Delta$ )  $1100^{\circ}C$ .

Figure 15 gives the values of the activities of magnetite and lithium ferrite in the spinel phase, practically in equilibrium with pure hematite, as calculated by the formulas

$$\log a_{Fe_{3}O_{4}} = -\frac{1}{2} \int_{(p_{O_{2}}^{0})Fe_{3}O_{4+d}/Fe_{2}O_{3}}}^{(p_{O_{2}}^{0})Fe_{3}O_{4+d}/Fe_{2}O_{3}}} -\frac{1}{4} \int_{(p_{O_{2}}^{0})Fe_{0}/Fe_{3}O_{4}}}^{PO_{2}} d\log p_{O_{2}}}, \qquad (18)$$

 $\log a_{\mathrm{Li}_{0.5}\mathrm{Fe}_{2.5}\mathrm{O}_4} = p_{\mathrm{O}_2}$ 

$$-\frac{1}{8} \int_{(p_{0_2}^0)^{Fe_2O_3/Li_{0.5}Fe_{2.5}O_4}}^{p_{0_2}} \chi \times d\log p_{O_2}$$
(19)

It is evident that the solutions of lithium ferrite with magnetite, in equilibrium with hematite, have negative deviations from ideality over the entire range of concentration. As is to be expected, these deviations decrease with rise in temperature, so that at  $1100^{\circ}$ C the solutions are practically ideal. It is noteworthy that on going from the low-oxygen boundary to the high-oxygen boundary significant change (especially at 900°C) in the activity of the components of the spinel is accompanied by a negligibly small change in oxygen composition. The latter would not be detected by chemical analysis nor by measurement of lattice constant.

We have also calculated the activity of the components of wüstite solution coexisting with



FIG. 16. Values of the activity of the components of wüstite solution found in equilibrium with spinel solid solution. ( $\bullet$ ) 900°C; ( $\times$ ) 1000°C; ( $\triangle$ ) 1100°C.

spinel. Figure 16 shows the values of the activity of Li<sub>0.5</sub>Fe<sub>0.5</sub>O and stoichiometric wüstite "FeO" calculated according to the following formulas:

$$\log a_{\text{``FeO''}} = -\frac{1}{2} \int_{(p_{O_2}) \cdot \text{`FeO''}}^{(p_{O_2}) \cdot \text{FeO'} + \delta} \frac{1}{2} \int_{(p_{O_2}) \cdot \text{``FeO''}}^{(p_{O_2}) \cdot \text{``FeO''}} \frac{1}{2} \int_{(p_{O_2}) \cdot \text{FeO} + \delta}^{(p_{O_2}) \cdot \text{FeO''} + \delta} \frac{1}{3z - x} d\log p_{O_2}$$

 $\log a_{\mathrm{Li}_{0.5}\mathrm{Fe}_{0.5}\mathrm{O}} =$ 

$$\frac{1}{4} \int_{(p_{O_2})_{L_{i_2}Fe_{1-2}O_1+\delta}}^{(p_{O_2})_{L_{i_2}Fe_{1-2}O_1+\delta}} \left[ \frac{(1-\gamma)(1-2z)}{3z-x} - \frac{8(3-2x)}{3z-x} \right] \times d\log p_{O_2}.$$
(21)

In Eq. (20),  $(p_{O_2})^{"}_{FeO"}$  is the equilibrium oxygen pressure over the mixture of stoichiometric composition "FeO"  $\rightleftharpoons aFe + bFeO_{1+\delta'}$  $(p_{O_2})_{FeO_{1+\delta}}$  is the pressure of oxygen over wüstite inequilibrium with magnetite, and  $(p_{O_2})_{Li_2Fe_{1-2}O_{1+\delta}}$ is the pressure of oxygen over a wüstite phase of arbitrary composition in equilibrium with spinel. In Eq. (21), the lower limit of integration corresponds to the pressure of oxygen over pure orthoferrite which is in equilibrium with the spinel phase. The quantity  $(p_{0_2})_{\text{Li}_{0.5}\text{Fe}_{0.5}\text{O}}$  was obtained by extrapolating the  $\Delta \hat{H}_{0_2} = f(z)$  curve to z = 0.5.

by extrapolating the  $\Delta H_{O_2} = f(z)$  curve to z = 0.5. As shown in Fig. 16, solid solutions of  $\text{Li}_{0.5}\text{Fe}_{0.5}\text{O}$  and  $\text{FeO}_{1+\delta}$  are characterized by negative deviations from ideality, the magnitudes of which practically do not change with temperature (athermal solutions). As is to be expected in the binary system Fe-O in pure  $\text{Li}_z\text{Fe}_{1-z}\text{O}_{1+\delta}$  at z = 0, the activity of "FeO" is noticeably less than 1.0 and decreases with an increase in temperature. This is a consequence of the nonstoichiometry of wüstite, in equilibrium with magnetite, which increases with a rise in temperature.

### References

- 1. J. SMIT AND H. P. J. WIJN, "Ferrites." Wiley, New York (1959).
- 2. P. B. BROWN, Nature, 170, 1123 (1952).
- 3. E. W. GORTER, Pat. U.S.A., No. 2,751,357.
- 4. E. S. SAVRANSKAYA, Y. D. TRETYAKOV, AND A. P. ERASTOVA, Vest. Moscow Univ., No. 3 (1971).
- 5. A. J. POINTON AND R. C. SAULL, J. Amer. Ceram. Soc. 52, 157 (1969).
- 6. J. THERY, Ann. Chem. 7, 207 (1962).
- 7. D. W. STRICKLER AND R. ROY, J. Amer. Ceram. Soc. 44, 5 (1961).
- 8. A. HOFFMANN, Naturwissenschaften 26, 431 (1938).
- 9. V. A. GRANIK, Y. G. METLIN, N. N. OLEYNIKOV, AND Y. D. TRETYAKOV, *Neorg. Mater.* 7, 129 (1971).
- 10. G. DEMOISSAN AND C. GLEITZER, C.r. Acad. Sci. Ser. C 272, 458 (1971).
- L. S. DARKEN AND R. W. GURRY, J. Amer. Chem. Soc. 67, 1398 (1945).
- 12. L. S. DARKEN AND R. W. GURRY, J. Amer. Chem. Soc. 68, 798 (1946).
- 13. A. E. VAN ARKEL, U. SPITSBERGEN, AND R. D. HEYDING, Can. J. Chem. 33, 446 (1955).
- 14. Y. D. TRETYAKOV AND N. N. OLEYNIKOV, J. Inorg. Chem. (USSR) 10, 1940 (1965).
- 15. Y. D. Tretyakov, Neorg. Mater. 1, 1928 (1965).
- N. N. OLEYNIKOV AND Y. D. TRETYAKOV, Neorg. Mater. 5, 528 (1969).